بسم الله الرحمن الرحيم

King Abdulaziz University
Engineering College
Department of Production and Mechanical System Design

MENG 470 Mechanical Vibrations

Final Exam
Closed-book Exam
Monday: 30/6/1425 H
Time Allowed: 120 mins

Name:	ID No.:

Question 1		25
Question 2		40
Question 3		35
TOTAL		100

قال الله تعالى : (تلك الدار الآخرة نجعلها للذين لا يريدون علوا في الأرض ولا فسادا والعاقبة للمتقين)

Instructions

1. This is a closed book and closed notes Opportunity to Shine
2. Show all work for partial credit.
3. Assemble your work for each problem in logical order.
4. Justify your conclusion. I cannot read minds.

Q1. Indicate whether each of the following statements is **true** or **false**:

1. The amplitude of an undamped system will not change with time.
2. A system vibrating in air can be considered a damped system.
3. The equation of motion of a single degree of freedom system will be the same whether the mass moves in a horizontal plane or an inclined plane.
4. When a mass vibrates in a vertical direction, its weight can always be ignored in deriving the equation of motion.
5. The principle of conservation of energy can be used to derive the equation of motion of both damped and undamped systems.
6. The damped frequency can in some cases be larger than the undamped natural frequency of the system.
7. The damped frequency can be zero in some cases.
8. The natural frequency of vibration of a torsional system is given by $\sqrt{k_T / J}$, where k_T and J denote the torsional spring constant and the polar mass moment of inertia, respectively.
9. The undamped natural frequency of a system is given by $\sqrt{g / \delta_{st}}$ where δ_{st} is the static deflection of the mass.
10. For an undamped system, the velocity leads the displacement by $\pi / 2$.
11. The motion diminishes to zero in both underdamped and overdamped cases.
12. The logarithmic decrement can be used to find the damping ratio.
13. In torsional vibration, the displacement is measured in terms of linear coordinate
14. The phase angle of the response depends on the system parameter *m*, *c*, *k*, and ω .
15. During beating, the amplitude of the response builds up and then diminishes in a regular pattern.
16. The *Q*-factor can be used to estimate the damping in a system.
17. The amplitude ratio attains its maximum value at resonance in the case of viscous damping.
18. Damping reduces the amplitude ratio for all values of the forcing frequency.
19. The unbalance in a rotating machine causes vibration.
20. The normal modes can also be called principal modes.
21. The generalized coordinates are linearly dependent.
22. Principal coordinates can be considered as generalized coordinates.
23. The vibration of a system depends on the coordinate system.
24. The nature of coupling depends in the coordinate system.
25. The magnification factor is the ratio of maximum amplitude and static deflection.
26. The response will be harmonic if excitation is harmonic.

27. The principal coordinates avoid both static and dynamic coupling.
28. The use of principal coordinates helps in finding the response of the system.
29. The mass, stiffness, and damping matrices of a two degree of freedom system are symmetric.
30. The characteristics of a two degree of freedom system are used in the design of dynamic vibration absorber.
31. A semidefmite system cannot have nonzero natural frequencies.
32. During free vibration, different degrees of freedom oscillate with different amplitudes.
33. The modal vectors of a system denote the normal modes of vibration.
34. The vibration of a system under external forces is called damped vibration.
35. When a two degree of freedom system is subjected to a harmonic force, the system vibrates at the frequency of applied force.
36. When the forcing frequency is equal to one of the natural frequencies of the system, a phenomenon known as *beating* occurs.
37. For a damped multidegree of freedom system, all the eigenvalues can be complex.
38. The amplitudes and phase angles are determined from the boundary conditions of the system.
39. A semi definite system has at least one rigid body motion.
40. The elastic coupling is also known as dynamic coupling while the inertia coupling is also known as static coupling.
41. The equations of motion of a system will be coupled when principal coordinates are used.
42. The vibration of a system under initial conditions only is called forced vibration.
43. The number of degrees of freedom of a vibrating system depends only on number of masses.
44. The equations of motion of a two degree of freedom system are in general coupled.
45. The stiffness matrix of a system is always symmetric and positive definite.
46. For a multidegree of freedom system, one equation of motion can be written for each degree of freedom.
47. Lagrange's equation cannot be used to derive the equations of motion of a multidegree of freedom system.
48. The mass, stiffness, and damping matrices of a multidegree of freedom are always symmetric.
49. A multidegree of freedom system can have six of the natural frequencies equal to zero
50. The mass matrix of a system is always symmetric and positive definite.

Answers:

	True	Flase
1.	O	O
2.	O	O
3.	O	O
4.	O	O
5.	O	O
6.	O	O
7.	O	O
8.	O	O
9.	O	O
10.	O	O
11.	O	O
12.	O	O
13.	O	O
14.	O	O
15.	O	O
16.	O	O
17.	O	O
18.	O	O
19.	O	O
20.	O	O
21.	O	O
22.	O	O
23.	O	O
24.	O	O
25.	O	O
26.	O	O
27.	O	O
28.	O	O
29.	O	O
30.	O	O
31.	O	O
32.	O	O
33.	O	O
34.	O	O
35.	O	O
36.	O	O
37.	O	O
38.	O	O
39.	O	O
40.	O	O
41.	O	O
42.	O	O
43.	O	O
44.	O	O
45.	O	O
46.	O	O
47.	O	O
48.	O	O
49.	O	O
50.	O	O

Q2. Consider the system shown in Figure 1 where m_1 = 30 kg, m_2 = 2 kg, k = 15 N/m, l=2m, $f(t)$ = 10 sin(5t) N.

(a) What's the degree of the system?

(b) Write the equation of motion of the system in matrix form.

(c) Is the system statically or dynamically coupled or both.

(d) Find the natural frequencies and corresponding mode shapes.

(e) Calculate the normalized eigenvectors of the system.

(f) Write down the matrix form.

(g) Decouple the coupled equations using modal transformation.

(h) Recover the physical degrees of freedom from the modal degree of freedom.

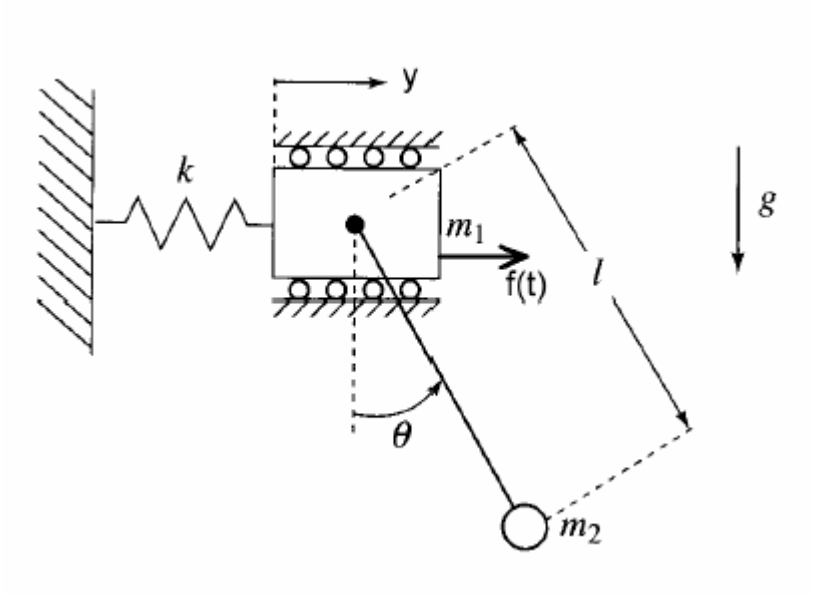

Figure 1

Q3. Consider a cable shown in Figure 2 that has one end fixed and the other end free to slide along a smooth vertical guide. The free end cannot support a transverse force so that we have:

$$\frac{\partial \omega(L,t)}{\partial x} = 0$$

The cable length L=100m is made out of steel with a uniform density ρ=7.8X10^{3} kg/m^{3}, and constant cross sectional area A=7.854X10^{-5} m^{2}; and it is under tension of T=10,000 N.

Calculate the natural frequencies and mode shape of the cable. Plot the first four made shapes (Normalized the mode shapes so that its maximum amplitude is one).

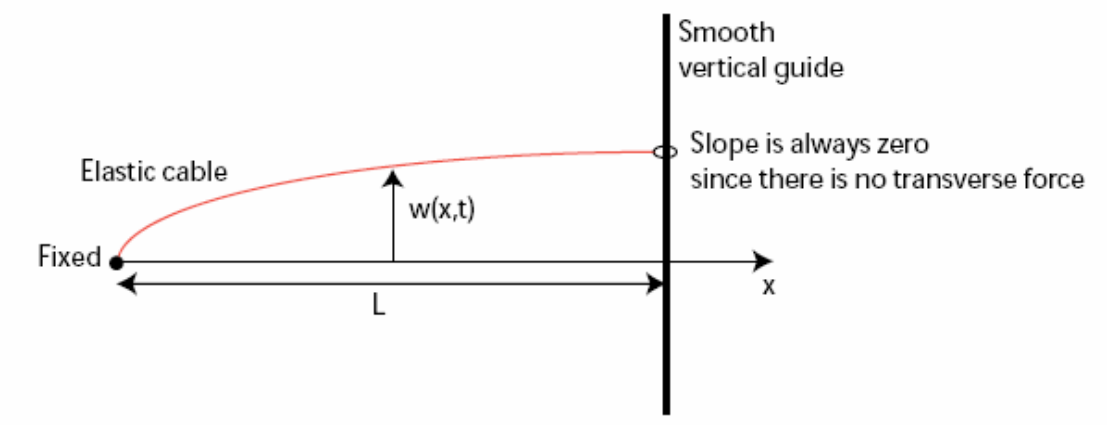

Figure 2