

Q1. Use Lagrange's equation to find the equation of motion for the system shown in Figure 1. The variables $y_1(t)$ and $y_2(t)$ represent known positions as a function of time so x is the only unknown quantity. Let $k_1 = 50$ N/m, $k_2=20$ N/m, $c = 2$ N-s/m, and $m= 10$ kg.

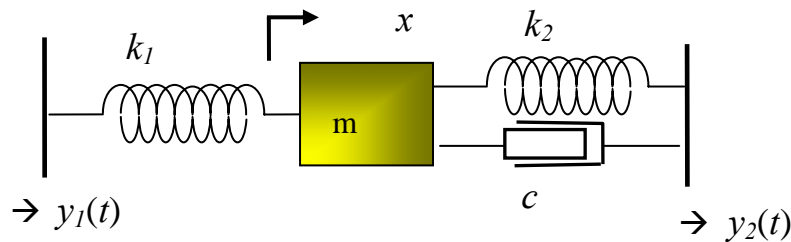


Figure 1

Q2. For the system shown in Figure 2:

1. Use Newtonian approach to find the equation of motion
2. Use Lagrange's equation to find the equation of motion
3. Find the natural frequencies and mode shapes.

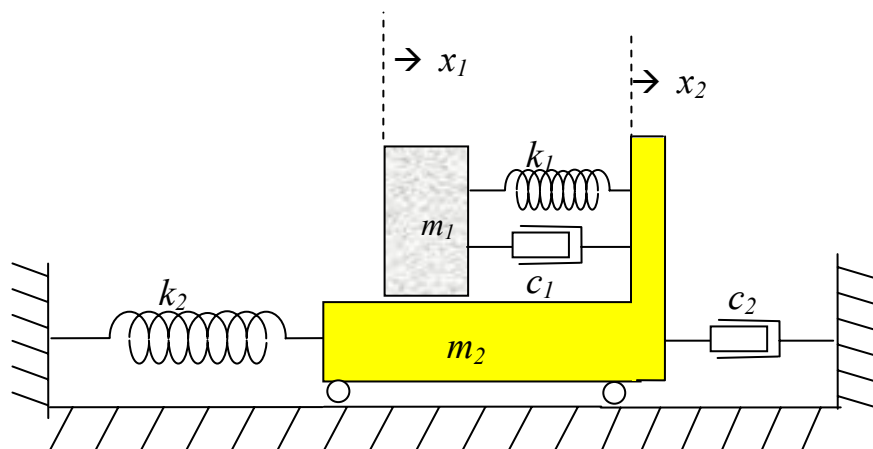


Figure 2

Q3. Use Lagrange's equation to find the equation of motion for the pendulum shown. Here $y(t)$ is known function of time. Use small angle theory to linearize the EOM in terms of θ .

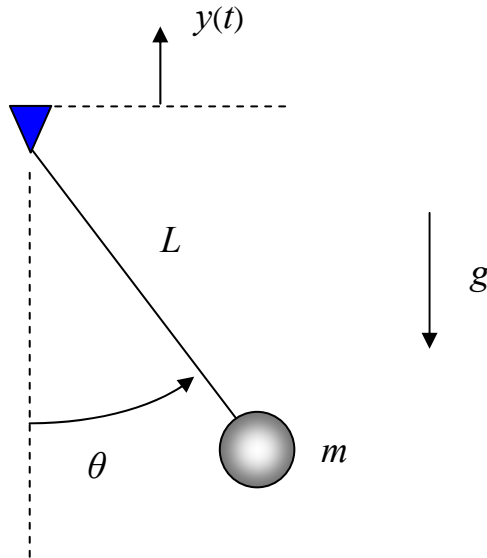


Figure 3

Q4. For the system shown in Figure 4:

- Use Newtonian approach to find the equation of motion
- Use Lagrange's equation to find the equation of motion
- Find the natural frequencies and mode shapes.
- If $c=0$, model the system as SDOF systems using modal transformation.

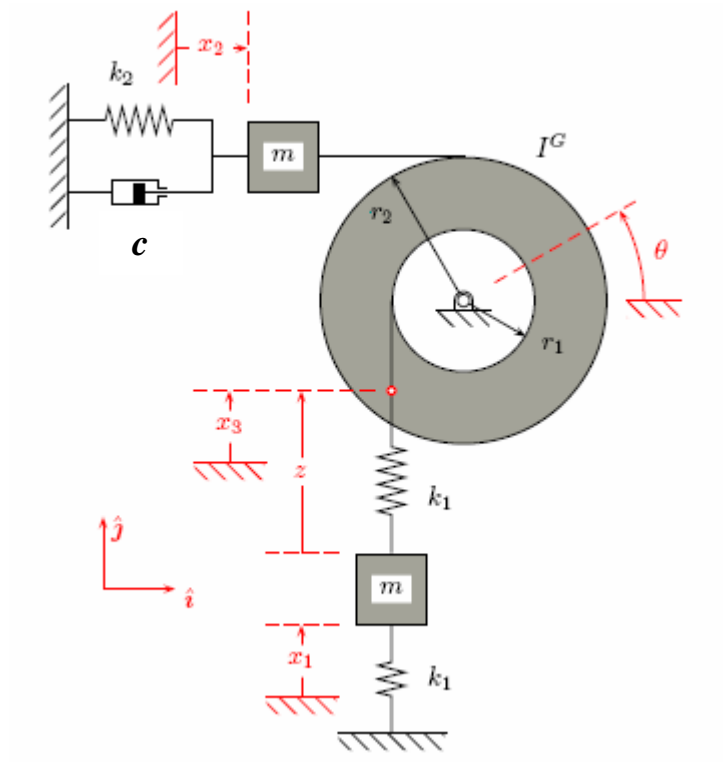


Figure 4